

Q. Find x where $0 < x < 1386$

- ① x is even $x \equiv 0 \pmod{2}$
- ② $x \equiv 2 \pmod{9}$
- ③ $x \equiv 1 \pmod{11}$
- ④ $x \equiv 4 \pmod{7}$

$$\gcd(\text{of all } \# \text{ of } n) = 1$$

$$m_1 = 693$$

$$693x = 1 \text{ in } \mathbb{Z}_2$$

$$1x = 1 \text{ in } \mathbb{Z}_2$$

$$x_1 = 1$$

$x_1 = 1$ and not 3 (you live inside \mathbb{Z}_2). It will not affect the final ANSWER since $c_1 = 0$

$$m_2 = 154$$

$$154x = 1 \text{ in } \mathbb{Z}_9$$

$$1x = 1 \text{ in } \mathbb{Z}_9$$

$$x_2 = 1 \text{ again } x_2 = 1 \text{ in } \mathbb{Z}_9$$

$$m_3 = 126$$

$$126x = 1 \text{ in } \mathbb{Z}_{11}$$

$$5x = 1 \text{ in } \mathbb{Z}_{11}$$

$$x_3 = 9$$

$$m_4 = 198$$

$$198x = 1 \text{ in } \mathbb{Z}_7$$

$$2x = 1 \text{ in } \mathbb{Z}_7$$

$$x_4 = 4$$

$$X = m_1 x_1 c_1 + m_2 x_2 c_2 + m_3 x_3 c_3 + m_4 x_4 c_4 \pmod{1386}$$

$$= (2 \times 154 \times \boxed{1}) + (1 \times 126 \times 9) + (198 \times 4 \times 4) \pmod{1386}$$

$$= \boxed{452}$$